Exercise 8

Yes or No? If No, give a reason. Assume that a and b are nonzero real numbers.

- (a) Is the distance between any two different real numbers always positive?
- (b) Is the distance between a and b the same as the distance between b and a?

Solution

- (a) Yes.
- (b) Yes.

The formula for the distance between two numbers on the number line is given by

$$d(a,b) = |b - a|.$$

Because of the absolute value sign, d(a, b) is always positive, and the order doesn't matter.

$$d(b,a) = |a - b| = |-(b - a)| = |b - a| = d(a,b)$$